

2. This is an arithmetico-geometric sequence.

Let,

$$S = \frac{1}{3} + \frac{2}{9} + \frac{3}{27} + \frac{4}{81} + \dots$$

Thus,

$$3S = 1 + \frac{2}{3} + \frac{3}{9} + \frac{4}{27} + \dots$$

Subtracting  $S$  from  $3S$  gives

$$2S = 1 + \frac{1}{3} + \frac{1}{9} + \frac{1}{27} + \dots$$

Thus,  $2S$  is an infinite geometric series with first term 1 and common ratio  $\frac{1}{3}$ . Using the formula for the sum of an infinite geometric series, we get that

$$2S = \frac{1}{1 - \frac{1}{3}} = \frac{1}{\frac{2}{3}} = \frac{3}{2}. \text{ This makes } S = \frac{\frac{3}{2}}{2} = \boxed{\frac{3}{4}}$$